

Neptun code:

Name:

Midterm 1

1. Construct a context free grammar for the following language:

$$L = \{ca^i b^j c \mid i, j \geq 0; i \neq j\}.$$

Neptun code:

Name:

2. (a) Is the class of context-free languages closed under the intersection operation? Prove your claim. (We have proved this in class.)

(b) Is the class of context-free languages closed under the union operation? Prove your claim. (We have proved this in class.)

Neptun code:

Name:

3. Prove that the language $L = \{a^i b^{i^2} c^i \mid i \geq 1\}$ is not context-free.

Neptun code:

Name:

4. Construct a Turing machine that recognizes the following language:

$$L = \{a^i b^{i^2} \mid i \geq 1\}$$

You don't have to draw a diagram, or give the δ function, just give a clear description how the machine works.